Comparing DSP Software Performance Prediction Models at Source Code Level — From Analytical to Statistical

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Abstract: Efficient performance prediction at source code level is essential in reducing the turnaround time of software development, particularly when the source code is subject to changes due to modification of problem specification. In this paper, we investigate and compare five performance prediction models from practical standpoint to determine the usefulness of these models. To verify the effectiveness of these models, we select a set of functions from PHY DSP Benchmark and TIC64 DSP processor for experiment. Comparing the predicted performance to the actual measured execution time, we observed that the relative prediction error generated from two of the five models are low and can thus be used for practical purposes.

Key words: Performance prediction, source code level, analytical model, statistic model.

1. Introduction

Performance prediction is an essential phase of DSP software development. It can be carried out at either the source code or lower level. Prediction at source level is much faster because it does not require the code to be compiled and executed. Thus, performance prediction at source code level helps reduce the turnaround time of software development especially when the source code must be modified due to changes in problem specification [1]-[20].

Over the past few years, we have separately investigated and developed five different models to estimate the execution time of DSP software at source code level. The formulations of these models are presented in section 2. To determine the effectiveness of these models in practice, we need to compute the predicted execution time of practical DSP application software and compare the computed result with experimentally measured data.

To this end, we have chosen eight most frequently used functions from the Long Term Evolution or LTE Uplink Receiver, a major part of the PHY benchmark [10] as the testing set of samples. PHY is an open-source benchmark developed by Chalmers University of Technology of Sweden and Ericson. It provides a realistic implementation of the baseband processing for an LTE mobile base station. Its source code is written in C and can be freely downloaded from [19]. In choosing the set of samples for the testing set, we used gprof, a popular profiling tool in UNIX, to make sure that the selected set is indeed the most frequently executed kernel functions in the PHY benchmark.

In Section 2 below, we provide a summary description of our five prediction models. Section 3 discusses the experimental procedures including how experimental results are gathered and organized. Section 4
discusses how the experimental results are used as a basis to predict the performance of whole system, i.e., the entire PHY benchmark application. Sections 5 presents related work reported by others. Sections 6 discusses the factors that affect the effectiveness of the five models.

2. Prediction Models

In this section, we discuss our five source code level prediction models presented in this paper, which includes a simple analytical model, an enhanced version of the simple analytical model, a precise analytical model taking into consideration the hardware-specific features, a statistical model using linear regression, and a comprehensive model combining both analytical and statistical models.

All five models focus on predicting the execution time of loops because loop execution alone predominates the total execution time of the entire DSP application. In fact, as reported in [13], loop execution takes up 70% execution time of the selectable mode vocoder application.

2.1. Simple Analytical Model

The simple analytical model is based on our earlier work on DSP processor [12]. We use a simple formula to calculate the loop execution time in terms of the clock cycles. Considering a two-level nested loops, the predicted execution time or PET can be expressed as follows:

$$\text{PET} = N_{outer} \times (L_{outer} + N_{inner} \times L_{inner})$$ (1)

where $N_{inner}$ and $N_{outer}$ are the numbers of iterations of the inner and outer loops; $L_{inner}$ and $L_{outer}$ are the numbers of statements in the inner loop and the outer loop, respectively.

2.2. Enhanced Analytical Model

Compared to the measured values, we observed that the simple analytical model tends to under-predict the performance for most of the samples being investigated. The major reason is that the inner loops of those samples make calls to some small complex functions which incur extra execution time not fully accounted for in the simple analytic model. If the assembly code of a simple sample is known, we can find the ratio of its inner loop body length in assembly code to the length of the source code. This ratio can then be used to adjust the predicted time of those under-predicted testing samples. For example, in our experiment we select a simple loop from sample #31 cholsolve_4xX_complex and find the ratio equals 3. We then multiply $L_{inner}$ by 3 in (1) to compute the PET or predicted execution time of those testing samples that under-predict the performance.

2.3. Precise Analytical Model

Based on our earlier work on source level loop optimization [11] we proposed a precise analytical model for performance prediction, which is machine-dependent and needs detailed hardware information such as the resource limitation of parallel function units and the latencies of instructions. With the understanding that the source code is written in C, the algorithm of the model is listed below:

1) Decomposing C statements in the innermost loop to DSP operations.
2) Building the data dependency graph DDG of DSP operations under the limitation of resources and instruction latencies.
3) Optimizing the inner loop body based on DDG with list scheduling or source level software pipelining [11].
4) Using the length of optimized loop body to replace $L_{inner}$ in simple analytical model to calculate the predicted execution time.

Fig. 1 presents an example of TI C64 DSP processor. The latencies of its memory load, multiply, and branch instructions are 5, 2, and 6 clock cycles respectively; the rest of instructions executes in one clock cycle. Fig. 1(a) shows the source code of a simple loop in chest function of PHY, Fig. 1(b) and (c) show the DSP operations inside the loop body from the C statements and the result of list scheduling. Fig. 1(d) is the result after source level software pipelining in which $L_{inner} = 1$.

\[ i=0 \]
\[
\text{for } (i = \text{used sc}; i < n; i++) \{
\text{out}[i].re = 0;
\text{out}[i].im = 0;
\}
\]  

(a) C source code

\[
\text{st 0, out}[i].re
\text{st 0, out}[i].im,
i++
\text{if } i = n, \text{quit}
\]

(b) DSP operations in loop body

\[
i = 0
\text{st 0, out}[i].re, \text{st 0, out}[i].im, i++
\text{if } i = n, \text{quit}
\]

(c) After list scheduling

\[
i = 0
\text{st 0, out}[i].re, \text{st 0, out}[i].im, i++
\text{if } i = n, \text{quit}
\text{st 0, out}[i].re, \text{st 0, out}[i].im, i++
\]

(d) After software pipelining

Fig. 1. Example of precise analytical model.

2.4. Statistic Model

Our statistical model uses the popular statistic tool IBM SPSS-23 to perform multiple linear regression [5]. SPSS-23 generates (2) below to predict the execution time for each testing sample.

\[
PET = b_0 + \sum_{j=1}^{p} b_j X_j
\]  

(2)

where $PET$, the predicted execution time is the dependent variable; $X_1, X_2, ..., X_p$ are independent variables representing attributes of the corresponding testing sample; and $b_0, b_1, b_2, ..., b_p$ are coefficients generated from attributes of the training samples by SPSS. The attributes of all training samples are listed in Table 1.

We take all five functions with different input data from the tele-communication group of EEMBC [18] and all eight functions of SMV benchmarks [4] as the samples of training set. EEMBC benchmark is an industry standard for embedded processors and software developed by the Embedded Microprocessor Benchmark Consortium, a non-profit organization [18]. SMV benchmark is developed by us in 2006 which consists of eight kernels chosen from the Selectable Mode Vocoder (SMV) application program for 3G wireless communications. The testing set contains eight samples from PHY same as we use for analytical models.

We gather 17 static attributes from the source code of the training and testing sets as shown in Table 1.
Below is the list and description of those attributes.

1) Number of statements in a sample.
2) Number of statements in the inner loops.
3) Number of statements in the outer loop which excludes the statements in the inner loops.
4) Number of iterations of the inner loops.
5) Number of iterations of the outer loop.
6) Number of loops, which includes all loops in the sample.
7) Number of levels of nested loop.
8) Number of total iterations, which equals the number of iterations of the outer loop * the number of iterations of inner loop.
9) Number of complex variables of inner loop.
10) CC*, a new metric we defined in 2006 [4] to measure code complexity based on Cyclomatic Complexity CC. A program can be graphically depicted by a control-flow graph. In a control-flow graph, CC = e-nn+np+1, where e, nn and np denote the number of edges, nodes, and connected components, respectively. We extended the definition of CC by taking into consideration of instruction level parallelism of the complex nested levels of loops and conditional branches. The

### Table 1. Attributes of Training and Testing Samples

<table>
<thead>
<tr>
<th>No.</th>
<th>Function name</th>
<th>Back-annotated Attributes</th>
<th>Attributes</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Bench mark</td>
<td></td>
</tr>
<tr>
<td>25</td>
<td>inf</td>
<td>10 12000 0 9 2 1 1200 0 2 3 1 0 5 1 9600 4800 10800 80431</td>
<td></td>
</tr>
<tr>
<td>26</td>
<td>softmax</td>
<td>18 43200 6 1 14 1 2 259200 2 8 2 1 5 1 4800 4800 362800 10374917</td>
<td></td>
</tr>
<tr>
<td>27</td>
<td>fft</td>
<td>40 10 700 17 17 1 3 7000 2 5 0 0 3 1 2400 2400 119000 110922</td>
<td></td>
</tr>
<tr>
<td>28</td>
<td>chest</td>
<td>10 3 500 0 6 2 1 900 10 4 0 0 5 1 4800 4800 5400 3423</td>
<td></td>
</tr>
<tr>
<td>29</td>
<td>fft</td>
<td>38 10 700 17 17 1 3 7000 4 5 0 0 3 1 2400 2400 119000 109975</td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>ant_comb</td>
<td>29 1 1200 0 29 1 1 1200 1 8 7 0 4 1 4800 4800 34800 479246</td>
<td></td>
</tr>
<tr>
<td>31</td>
<td>matrix_u_a_hermite_pla</td>
<td>60 3 3 1 50 3 1 9 8 21 11 0 5 1 128 64 450 3143</td>
<td></td>
</tr>
<tr>
<td>32</td>
<td>matrix_mult_4x complexes</td>
<td>27 3 3 1 26 1 2 9 3 8 7 0 4 1 128 64 234 1569</td>
<td></td>
</tr>
</tbody>
</table>
modified cyclomatic complexity $CC^*$ equals the sum of numbers of loops and branches in the program, plus the number of nested levels of loops and branches.

11) Total number of function calls inside a sample.
12) Total number of branches inside a sample.
13) Total number of input variables of a sample.
14) Total number of output variables of a sample.
15) Total data size of all input variables measured in bytes.
16) Total data size of all output variables measured in bytes.
17) $N_{inner} \cdot L_{inner}$, the major parameter used to predict performance in analytical models.

2.5. Comprehensive Prediction Model

We proposed an approach [5], which is referred to as the comprehensive model in this paper. The model combines the statistical model with the analytical model described in sections 2.4 and 2.1, respectively, and it uses some heuristics, as described below:

1) Adding to the model a new independent variable Repeating Times $RT$ as an additional attribute. Table 1 shows that the execution time of some samples, such as samples 1, 18, and 23, in the training set is very small relative to that of other samples. By repeating $RT$ times, the wide range of variation among samples’ execution time can be reduced. An iterative algorithm has been designed to determine the best value of $RT$ for the training set [5]. With this new attribute, SPSS generates (3) which can be used to predict the execution time of testing samples.

$$APET_k = (b_0 + \sum_{j=1}^{n} b_j X_{jk}) + b_{RT} RT_k$$

where $APET_k$ is the adjusted predict execution time of testing sample $k$ generated by SPSS, $X_{jk}$ is the value of $j$th-attribute in that sample. The value of $N_{inner} \cdot L_{inner}$ from analytical model are used as the values for $RT_k$ to determine the execution time of the $k$th sample of the testing set by using (4) below.

$$PET_k = \frac{APET_k}{RT_k}$$

From the source code and assembly code of PHY kernel functions we notice that their kernel functions are quite different from the typical DSP functions in EEMBC and SMV, e.g. there is no complex variables in EEMBC and SMV functions. For this reason, we select a typical PHY kernel function, sample #31 with three complex variables, as a new member of the training set.

2) From the analytical model, we realize that some function calls and some optimization technique such as software pipelining can have large impact on execution time. To compensate these factors, we have designed and employed two heuristics to adjust $RT_e$.

3. Experiments

We use TI C64 DSP processor as the hardware platform for our experiments. All samples in the training and testing sets are compiled by TIC64 compiler and run on TIC64 simulator. The execution time as the performance metric is gathered from that simulator in terms of number of CPU clock cycles. We use relative errors $RE$ and average absolute relative error $ARE$ to describe the prediction accuracy. $RE$ and $ARE$ are defined as follows:
Table 2. Experiment Results of Five Models

<table>
<thead>
<tr>
<th>Testing Sample</th>
<th>Name</th>
<th>No.</th>
<th>simple</th>
<th>analytic</th>
<th>enhanced</th>
<th>analytic</th>
<th>precise</th>
<th>analytic</th>
<th>statistic</th>
<th>comprehensive</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mf</td>
<td>25</td>
<td>-71.0%</td>
<td>-37.0%</td>
<td>-18.2%</td>
<td>-37.8%</td>
<td>-34.5%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>softe_demap</td>
<td>26</td>
<td>-63.8%</td>
<td>6.2%</td>
<td>15.8%</td>
<td>-75.9%</td>
<td>-9.4%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>ifft</td>
<td>27</td>
<td>7.3%</td>
<td>7.3%</td>
<td>23.9%</td>
<td>-51.3%</td>
<td>5.5%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>chest</td>
<td>28</td>
<td>57.8%</td>
<td>57.8%</td>
<td>-3.0%</td>
<td>689%</td>
<td>-22.4%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>fft</td>
<td>29</td>
<td>8.2%</td>
<td>8.2%</td>
<td>25.0%</td>
<td>-52.8%</td>
<td>7.9%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>ant_comb</td>
<td>30</td>
<td>-92.7%</td>
<td>-78.2%</td>
<td>-47.7%</td>
<td>-99.8%</td>
<td>0.0%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>matrix_a_a_herminte_</td>
<td>32</td>
<td>-83.4%</td>
<td>-50.2%</td>
<td>-34.8%</td>
<td>-1617%</td>
<td>-28.3%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>matrix_mult_4xX_com</td>
<td>33</td>
<td>-79.9%</td>
<td>-40.1%</td>
<td>-7.1%</td>
<td>-1897%</td>
<td>-25.5%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>ARE</td>
<td></td>
<td>58.0%</td>
<td>35.6%</td>
<td>21.9%</td>
<td>565%</td>
<td>16.7%</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\[
RE = \left(\frac{\text{Predicted} - \text{Actual}}{\text{Actual}}\right) \times 100\% \tag{5}
\]

\[
ARE = \left(\frac{\sum_{i=1}^{M} |\text{Relative error}|}{M}\right) \tag{6}
\]

In (5) and (6), the actual values are measured in experiments and M is the total number of testing samples, which equals 8. Table 2 presents the experimental results in terms of RE and ARE of all five models.

### 4. Predict the Performance of Whole System with Gprof

We use gprof, a popular UNIX profiling tool, for our experiments. In order to use gprof, we need to enable profiling while compile our programs, and then execute the programs on the host computer to produce the profiling data. Finally run gprof on the profiling data file to produce the analysis information, which includes function call graph and an overview of the execution time for all the functions. We use the called times of the major functions generated by gprof and the predicted clock cycles for these functions to compute the predicted performance of the whole system. Equation (7) shows how the predicted execution time of all major functions is computed. Comparing it with the actual measured system execution time, we can calculate the relative prediction errors for all five models. The results for both the predicted execution time of all major functions and the relative prediction errors for all five models are presented in Table 3.

The predicted execution time of all major functions

\[
\text{predicted execution time} = \sum_{i=1}^{N} \left(\text{predicted execution time}_i \times \text{called times}_i\right)
\]

where called times\(_i\) is the number of time the \(i\)th function gets called.

### 5. Related Work

Reference [6] uses analytical modeling to predict the execution times of parallel programs. Reference [21] builds DDGs of basic blocks of DSP assembly code generated from C statements, uses list scheduling to determine their clock cycles, and then multiplies the number of execution time of those C statements collected by a host computer to predict the performance of a DSP processor. Based on programs ran on many different machines, [16] gathers program characteristics such as instruction mix, distribution of operands, and basic block size, then makes use of the squared Euclidean distance to identify the similarities among programs and
uses the result to predict the performance of these programs on different hardware. Reference [3] collects certain static and dynamic microarchitecture-independent characteristics including instruction mix and cache miss rate from SPEC 2000 benchmark programs and uses their similarity to predict program performance on different hardware using three different analytical models.

Many articles use various statistical approaches to predict the performance of software on target computers. For example, [20] uses various types of instructions as attributes for multiple linear regression, [17] uses a regression-tree-based modeling, and [1] uses a nonlinear regression model. References [10] and [8] use various machine training approaches to predict software performance on multi-core processors. Reference [7] uses both static attributes such as numbers of different types of instructions and dynamic attributes such as number of cache misses for regression. Reference [2] proposes cross-architecture performance prediction. It is a machine training based technique using both static and dynamic attributes from many programs from some/different benchmarks. They use R package to implement the regression and predict the execution time on a GPU from a single thread CPU with an average error of 26.9%. Using a constrained locally sparse linear regression algorithm, [15] proposes a training-based analytical cross-platform performance prediction.

### Table 3. Performance Prediction of Whole System

<table>
<thead>
<tr>
<th>Function</th>
<th>Actual measured values</th>
<th>Simple analytic model</th>
<th>Adjusted analytic model</th>
<th>Precise analytic model</th>
<th>Comprehensive model</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Actual execution time</td>
<td>called times from gprof</td>
<td>Total execution time</td>
<td>Total execution time in whole system</td>
<td>Total execution time in whole system</td>
</tr>
<tr>
<td>mf</td>
<td>70,431</td>
<td>24</td>
<td>1,690,344</td>
<td>20,400</td>
<td>489,600</td>
</tr>
<tr>
<td>soft_demap</td>
<td>10,374.917</td>
<td>1</td>
<td>10,374.917</td>
<td>3,758,484</td>
<td>3,758,484</td>
</tr>
<tr>
<td>fft</td>
<td>109,922</td>
<td>60</td>
<td>6,555,320</td>
<td>199,000</td>
<td>7,140,000</td>
</tr>
<tr>
<td>chest</td>
<td>3,423</td>
<td>24</td>
<td>82,152</td>
<td>5,400</td>
<td>129,600</td>
</tr>
<tr>
<td>fft</td>
<td>109,975</td>
<td>24</td>
<td>2,639,400</td>
<td>199,000</td>
<td>2,856,000</td>
</tr>
<tr>
<td>ant_comb</td>
<td>479,246</td>
<td>36</td>
<td>17,252,856</td>
<td>34,803</td>
<td>1,252,908</td>
</tr>
<tr>
<td>matrix_a_a_hermite</td>
<td>3,143</td>
<td>2,400</td>
<td>7,543,200</td>
<td>522</td>
<td>1,252,800</td>
</tr>
<tr>
<td>matrix_mult_4x4X_con</td>
<td>1,569</td>
<td>2,400</td>
<td>3,756,600</td>
<td>336</td>
<td>758,400</td>
</tr>
<tr>
<td>total</td>
<td>50,003,789</td>
<td></td>
<td>17,637,792</td>
<td>319,80,360</td>
<td>42,466,574</td>
</tr>
</tbody>
</table>

Relative prediction error comparing with total 8 functions
-64.73%  -36.04%  -15.08%  -8.20%
Relative prediction error comparing with whole PHY system
-67.50%  -41.70%  -21.75%  -15.4%

**Note:** Total measured CP of 8 kernel functions = 50,003,789. Actual execution time of whole PHY = 54,266,642.

### 6. Discussion

1) Table 2 summarizes the experimental results of all five models investigated in this paper. From it we observe that the simple analytical model has large under-prediction errors, which is caused by large overhead in assembler code especially when those samples involve many function calls. However, we also observe that some samples have over-prediction problem. This is due to the shortened inner loop body of assembly code generated by the loop optimization of compiler. The enhanced analytical model can reduce the under-prediction errors if we can get the length ratio between \( L_{\text{inner}} \) of assembly code and source code.

2) To further improve the accuracy of performance prediction, even the precise analytical model needs detailed information of hardware. Nevertheless, its predicted errors, as shown in Tables 2 and 3, is much improved to reach the acceptable level.
3) Table 2 shows that the prediction errors of the statistical model are very large because the number of training samples used in the paper is small. Also, the values of attributes among different samples vary over a wide range.

4) The comprehensive model combines statistical and analytical approaches; it also adds some sample from PHY to the training set. As shown in Table 3, its prediction error becomes reasonably small to be in practice to predict the performance of the entire PHY system; this is shown in Table 3. It is the best among the five models investigated in this paper for predicting the DSP performance at source level.

5) Both the precise analytical and the comprehensive models can be combined with other works [14] to predict the performance of source code running on different hardware.

6) Currently we are working on a project using machine learning techniques to predict DSP performance at source code level.

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References


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