IWFPM: Interested Weighted Frequent Pattern Mining with Multiple Supports

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Abstract: Association rules mining has been under great attention and considered as one of momentous area in data mining. Classical association rules mining approaches make implicit assumption that items’ importance is the same and set a single support for all items. This paper presents an efficient approach for mining users’ interest weighted frequent patterns from a transactional database. Our paradigm is to assign appropriate minimum support (minsup) and weight for each item, which reduces the number of unnecessary patterns. Furthermore, we also extend the support-confidence framework and define an interest measure to the mining algorithm for excavating users’ interested patterns effectively. In the end, experiments on both synthetic and real world datasets show that the proposed algorithm can generate more interested patterns.

Key words: Data mining, frequent pattern mining, association rules technology, interest.

1. Introduction

Data mining aims to discover knowledge patterns hidden in large database. Several data mining approaches are used to extract interesting knowledge [1]. Like, association rule [2], the area being researched most actively, is a technique to detect the relation in the data. Classification [3] is used for identifying the different class existing in categorical labeled data, clustering [4] is a technique to group the data into clusters based on similarities among them. All these techniques may be applied widely according to the needs of the enterprise.

In the paper, we mainly study the association rules technique, whose purpose is to search for the interesting correlations, associations between items in the data repositories. In the existing applications, the algorithms for mining frequent item sets can be classified into two types: Apriori-like methods and FP-growth-like methods. Among them, the Apriori-like methods are based on the well-known Apriori algorithm [2] and focus on reducing candidate item sets. The FP-growth-like methods are on the basis of FP-growth algorithm [5] and avoid generating candidate item sets by building a FP-tree, which overcome the bottlenecks of the Apriori-like algorithm. Later, references [6]–[9] have made corresponding improvement in time and space. However, these improved methods have discovered frequent patterns by setting fixed consistent minsup for all items and concerns are still unsolved.

The first concern is that all items are treated uniformly in previous approaches, but real items have different importance. For this reason, weighted frequent pattern mining algorithms have been suggested to filter interesting rules by attaching different weights to items [10]–[13]. High weights are attached to items...
of high importance and the unimportant rules are easily differentiated. Ahmed et al. [14] also introduce the
dynamic weight for each item, and propose the algorithm DWFPM (dynamic weighted frequent pattern
mining). Reference [15] extends prior research based on the Valency model and automates the process of
weight assignment by formulating a linear model that capturing relationships between items. The second
concern is that most traditional mining algorithms have used the single constant minsup, which bring “rare
item problem” dilemma, and how to set the reasonable minsup becomes a serious problem. If the minsup is
high, a lot of potential item sets are removed during the pruning process, whereas it may generate a huge
number of unnecessary item sets. For these problems, Liu et al. [16] have put forward the MS Apriori
Algorithm based on multiple supports for frequent pattern discovery. References [17], [18] use the
maximum constraint and propose a simple algorithm based on the Apriori approach for finding the
large-item sets and association rules under the constraint. Wang et al. [19] propose an array based tail node
tree structure (namely AT-Tree) to maintain transaction item sets, and a pattern-growth based algorithm
named AT-Mine for FIM over uncertain dataset. Yang et al. [20] propose the IA spam algorithm that not only
can handle a set of items at a time but also can incrementally mine across-streams sequential patterns.
Kiran et al. [21] also have presented an improved approach on account of the notion of “support difference”,
where each item is given suitable minsup to mine rare frequent patterns.

As the two problems mentioned above are not opposite, in further studies, for the sake of settling the two
considerations simultaneously, Duan et al. [22] propose the algorithm AMWARMS to excavate weighted
frequent patterns with multiple supports. However, the multiple supports considered in the algorithm is not
the frequency of different items but itemsets. Then, Zou et al. [23] come up with a new model of weighted
frequent patterns mining and design the algorithm DWARMMS, which allows the user to set different
weight and minsup for the item according to their importance and frequency in the database. Yun et al. [24]
present a new strategy WIP, which not only gives a balance between the two measures of weight and
support, but also considers weight affinity and support affinity between items within patterns.

Yet, these algorithms are all based on the support-confidence framework without taking the users’ real
preference into account. Therefore, this paper proposes an efficient algorithm IWFPM (Interested Weighted
Frequent Pattern Mining), and adds an interest measure reflecting users’ favors to the algorithm in that it
can excavate more users’ interest frequent patterns.

The remainder of paper is organized as follows. In Section 2, we provide some background information
on association rules technology. Section 3 develops the mining algorithm IWFPM, and extensive
experimental results are shown in Section 4. Finally, Section 5 reports the conclusion and future work.

2. Related Works

2.1. Definition of Association Rules

Association rules have been first initiated by Agrawal et al. [2] and continuing as the research hotspot in
data mining all the same. The basic terminology about association rules is as follows. Let  \( I = \{i_1, i_2, ..., i_n\} \) be
a unique set of items. A transaction database, \( T \), is a set of transactions and each transaction is denoted as a
tuple \( <tid, X> \), where \( tid \) is the identifier of the transaction and \( X \subseteq I \). We call \( X \) a k-pattern if it contains k
items. A frequent pattern is an implication of the form, \( X \Rightarrow Y \) that satisfying \( X \subseteq I \), \( Y \subseteq I \) and \( X \cap Y = \emptyset \),
holds in \( T \) with support \( s \) if \( s\% \) of the transactions in \( T \) contain \( X \cup Y \). Similarly, rule \( X \Rightarrow Y \) holds in \( T \) with
certainty \( c \) if \( c\% \) of transaction in \( T \) that support \( X \) and \( Y \). With regarding to support and confidence in
discovering the association rules, the user shall set the minimum support (minsup) and minimum
certainty (min conf) as critical values that providing the baselines for discovery. That is, for a rule \( R \), if
\( \text{sup}(R) \geq \text{min sup} \) and \( \text{conf}(R) \geq \text{min conf} \), there exists a pattern \( R \).
As association rules have been researched and applied in diverse ways. In this paper, we take the foundational association rules algorithms Apriori and FP-growth for example to explain the process of mining association rules in different angles.

### 2.2. Apriori Algorithm

Apriori algorithm employs an iterative level-wise search for generating frequent item sets. The most significant characteristic of Apriori approach is that it constitutes from the previous frequent item sets rather than all the data items accessed in the transaction when selecting candidate item sets. The frequent item sets refer to the item sets whose supports are greater than or equal to the user’s specified minsup. Here, \( C_k \) is the candidate item sets, where \( k \) is the number of item in the item set. Likewise, \( L_k \) represent a k-frequent item set. The Apriori algorithm executes as follows:

1. \( C_1 \) is generated.
2. \( L_k \) is generated from \( C_k \) by pruning the item sets.
3. \( C_{k+1} \) is generated by joining \( L_k \) with itself. Then, repeats the steps from 1) to 3) starting with \( k=1 \) till no more frequent item sets are found [3].

The process of mining frequent item sets using Apriori is depicted in Fig. 1.

![Fig. 1. The working of Apriori algorithm.](image)

As can be seen from the above, in the case of massive data, Apriori has two defects: 1) it has to repeatedly scan a large amount of original database in order to check whether a candidate item set is frequent, and time cost is very high; 2) there is a huge number candidate k-frequent item sets generated by the connection of k-1-frequent item sets so that space cost is also very high.

### 2.3. FP-Growth Algorithm

For figuring out the above issues, Han et al. [5] propose the frequent pattern tree (FP-tree) structure for storing compressed, crucial information about frequent patterns, and develop the FP-growth algorithm. There are two differences with Apriori algorithm: 1) generates no candidate item sets; 2) only needs to traverse database twice. Its procedures are as follows:

1. finds the frequent items and calculates their frequencies, then sorts items with frequency in descending order for each transaction;
2. constructs a novel FP-tree structure; 3) uses the FP-tree structure build conditional trees recursively for mining frequent item sets [25].

The process of FP-growth algorithm is shown in Fig. 2.
Fig. 2 illustrates that FP-growth algorithm applies a pattern growth method to avoid the costly candidate generation by concatenating frequent items in the FP-tree. Then we acquire the conditional pattern-base of each item from the FP-tree recursively, as is depicted in Table 1.

<table>
<thead>
<tr>
<th>Item</th>
<th>Conditional pattern-base</th>
<th>Conditional FP-tree</th>
<th>Frequent patterns</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>{(C:1),{B,C,E:1}}</td>
<td>{(C:2)}</td>
<td>A</td>
</tr>
<tr>
<td>E</td>
<td>{(B:1),{B,C:2}}</td>
<td>{(B:3,C:2)}</td>
<td>E</td>
</tr>
<tr>
<td>C</td>
<td>{(B:2)}</td>
<td>{(B:2)}</td>
<td>C</td>
</tr>
<tr>
<td>B</td>
<td>Ф</td>
<td>Ф</td>
<td>Ф</td>
</tr>
</tbody>
</table>

In view of the above analysis, though FP-growth algorithm has overcome disability of Apriori algorithm, there still exist deficiencies. First, it is not feasible to construct a main memory-based FP-tree if the database is large and sparse. Second, it needs to build a conditional pattern base and conditional sub-FP-trees for each shorter pattern, thus it is time and space consuming operation. Therefore, the paper presents an efficient approach IWFPM to extract more interest frequent patterns.

3. The Proposed Approach

In this section, weighted frequent pattern, weighted minsup and interest are described. Then, the efficient mining algorithm IWFPM for excavating more interesting weighted frequent pattern is given.

3.1. Definitions

3.1.1. Weighted frequent pattern

On the basis of the definition of association rules in section II, we redefine weighted frequent pattern in our approach. Analogously, \( I = \{i_1, i_2, \ldots, i_n\} \) is a set of items and \( W = \{w_1, w_2, \ldots, w_m\} (w_i \in [0,1]) \), a set of non-negative real numbers, which refers to the different importance of each item. After a single item has the weight, the item set containing the items also has the corresponding weight. A pair \( (X, w(X)) \) is called a weighted item set, where \( X \subseteq I \) and \( w(X) \subseteq W \). The weighted support of an item set \( X \), denoted as \( w_{sup}(X) = sup(X) \times w(X) \), where \( sup(X) \) is the percentage of the number of transactions in database containing \( X \), and the weight of item set \( X \) is defined as
Similarly, the weight support of item set \( X \cup Y \) is calculated as:

\[
w \sup(X \cup Y) = \frac{\prod_{k=1}^{\|X\cup Y\|} w(i_k)}{\sum_{k=1}^{\|X\cup Y\|} w(i_k)}, \ i_k \in X \cup Y
\]  

(2)

Therefore, weighted confidence of rule \( X \Rightarrow Y \) is defined as \( wconf(X \Rightarrow Y) = \frac{w \sup(X \cup Y)}{w \sup(X)} \), where \( X \subset I, Y \subset I \). At the same time, rules' definition has also changed when compared with the previous definition. \( X \Rightarrow Y \) is a valid rule if its weighted support \( w \sup(X \cup Y) \) and weighted confidence \( wconf(X \Rightarrow Y) \) satisfying minimum weighted support (minwsup) and minimum weighted confidence (minwconf).

### 3.1.2. Weighted minsup

In this definition, the minsup is not a single specified value that set according to users' experience, but a value determined by the importance and frequency of item in the database. Hence, for each item \( i_k \), the calculation of weighted minsup (\( MIS(i_k) \)) is as follows:

\[
MIS(i_k) = w(i_k) \times (\sup(i_k) - SD) \quad \text{when} \quad (\sup(i_k) - SD) > LS
\]  

\[
= w(i_k) \times LS \quad \text{otherwise}
\]  

(3)

where \( \sup(i_k) \) refers to support of item \( i_k \), support difference (SD) indicates the acceptable deviation of an item from its frequency, and \( LS \) refers to the user-specified least support. We define the least support (LS) mainly for preventing MIS value of each item from reaching 0 or lower. Least support is the lowest minsup that an item or item set needs to satisfy for being frequent, and LS takes a value in \([0, 1]\).

For a given database, the value of SD can be calculated as (4).

\[
SD = \alpha(1 - \beta)
\]  

(4)

where \( \alpha \) represents the parameter like mean, median, mode, maximum support of items and \( \beta \) ranges from 0 to 1, SD takes the value in \([0, \alpha]\).

Both \( \alpha \) and \( \beta \) play major role in determining SD. This paper, we select mean support of all items as \( \beta \). Therefore, after specifying MIS value for each item as (3), the frequent item sets are generated using (5).

\[
\begin{align*}
w \sup(X) &\geq \min(MIS(i_1), MIS(i_2), ..., MIS(i_k)), \ i_k \in X
\end{align*}
\]  

(5)

The Equation (5) guarantees the extraction of frequent item sets from frequent items, rare items.
efficiently. That is to say, a constant difference between support of item and their MIS can be confirmed irrespective of the support values. So it can be used in all kinds of datasets whose item supports vary widely.

3.1.3. Interest

Usually, the basic evaluations of association rules are support and confidence. However, there exists a problem, if the confidence of rule \( X \Rightarrow Y \) tells us that the possibility of \( X \) and \( Y \) appearing in the meantime is high, whether \( X \) accelerates the emergence of \( Y \). Reference [25], [26] has given the detailed explanation. The conclusion is that rule \( X \Rightarrow Y \) cannot correctly reflect the trend of appearance of \( Y \). Thus, we define the interest and add it to the mining algorithm based on the difference between information expressed by association rules and information supported by all original records.

The accuracy of information shown by association rule \( X \Rightarrow Y \) is determined by its confidence, while the information supported by all original records can be represented by \( \text{sup}(X) \). So we define the interest as (6).

\[
\text{Interest}_R = \frac{C_R - \text{sup}(Y)}{\max\{C_R, \text{sup}(Y)\}}
\]

where \( C_R \) is the confidence of rule \( \mid X \cup Y \mid / \mid X \mid \), \( X \Rightarrow Y \) is the support, right part of rule. Obviously, \( C_R \) and \( \text{sup}(Y) \) do not exist relationship in any quantity, therefore, \( \text{Interest}_R \) may be greater than or less than 0.

We introduce the denominator value as a normalization factor that making the interest be in -1 and 1, and this paper only considers the interest to be greater than 0. Then we again modify the definition of rule, namely a valid rule to be interest that its interest must meet the minimum interest pre-defined by users.

3.2. Algorithm

With the definition of weighted frequent pattern, weighted minsup, interest above, we now present the efficient algorithm, and introduces the interest as a measure to evaluate the frequent patterns mined to be interest or not.

**Algorithm**: IWFPM (Interested Weighted Frequent Pattern Mining)

**Require**: T: transaction dataset, W: weight of each item, SD: support difference, LS: least support, min wconf: minimum weighted confidence, min Interest: minimum interest

**Ensure**: Interest weighted frequent patterns

1) Generate candidate 1-itemset \( C_1 \)
2) Calculate weighted support \( \text{wsup} \) for item sets in \( C_1 \)
3) \( MIS = \text{calculate}_\text{-mis}(\text{wsup}, SD, LS) \)
4) \( L_i = \{<i> \mid i \in C_1, \text{wsup}(i) \geq MIS(i)\} \)
5) for \( k=2; L_{k-1} \neq \emptyset; ++k \) do
6) if \( (k = 2) \)
7) \( C_2 = \text{lev2}_\text{-gen}_\text{candidate}(C_1) \)
8) else
9) \( C_k = \text{gen}_\text{candidate}(L_{k-1}) \)
10) end if
11) for transaction \( t \in T \) do
12) \( C_i = \text{subset}(C_k, t) \)
for each candidate \( c \in C_t \) do

update \( \text{wsup}(c) \)

end for

end for

\( L_x = \{ c \mid c \in C_t, \text{wsup}(c) \geq \min(MIS(c)) \} \)

\( L = L \cup L_x \)

end for

Rules Set = \( \min \) \( \text{association}_\) \((L)\)

The algorithm has the following instructions.

1) \( MIS = \text{calculate}_\) \((\text{mis}(\text{wsup, SD, LS}))\) : the procedure for calculating MIS value of each item according to its \( \text{wsup, SD, LS} \).

2) \( C_2 = \text{lev2_gen_candidate}(C_1) \) : generates 2-frequent item sets. As there may be 1-infrequent item sets becoming the candidate of 2-frequent item sets, that is \( C_2 \) derives from \( C_1 \) rather than \( L \), therefore, generating the 2-candidate item sets require to be implemented solely.

3) \( C_k = \text{gen_candidate}(L_{k-1}) \) : generates candidate item sets.

4) \( C_t = \text{subset}(C_{k-1}, t) \) : generates all \( k-1 \) subsets of the candidate \( C_t \).

5) \( Rules \) Set = \( \min \) \( \text{association}_\) \((L)\) : produces the interest frequent patterns that meeting the minwconf and minInterest from frequent item sets in \( L \).

4. Performance Evaluation

In order to evaluate the IWFPM algorithm, the operating environment chosen is as follows: Intel (R) Xeon (R) CPU E7-4820@2.00 GHz, 32G memory, Linux O/S, and we use Matlab R2011b implement the algorithm. We also select two kinds of datasets: synthetic dataset and real world dataset. The synthetic dataset is the famous UCI dataset Mushroom that containing 119 items and 8124 transactions. The real world dataset is the processed log data, which is a week of log of the server of Chongqing Agricultural and Rural Information Network, and it contains 1590 items and 50192 transactions.

As each item in real world dataset refers to a page of website, we choose relative browsing time and access frequency as the two factors to measure the importance of the page. The weight of page \( i \) is defined as:

\[
w(i) = \frac{2 \cdot \text{time}(i) \cdot \text{freq}(i)}{\text{time}(i) + \text{freq}(i)}\]

Weights allocation of each item is shown in Fig. 3.

In the experiment, the proposed IWFPM approach requires two parameters, LS and \( \beta \). Therefore, first of all, the performance of IWFPM measured by elapsed time is evaluated by \( \beta \) value, and then we fix the LS value at 1%, 3% and 5%. The value of \( \alpha \) is defined as the mean of all items. Fig. 4(a) shows the performance of IWFPM at various \( \beta \) values for synthetic dataset. It can be observed that at low \( \beta \) value, the time consumption for mining weighted frequent patterns is high. When \( \beta \) is high, the time decreases, which is consistent with the single minimum support algorithm. Fig. 4(b) shows the performance of IWFPM at various \( \beta \) values for real world dataset.
Then, we compare the IWFPM algorithm to IMSApriori algorithm presented in reference [20]. As the two algorithms have the common parameters, LS and $\beta$, and the difference is that our method gives the weight for each item. Hence, as is shown in Fig. 5, we take $\beta=0.2$, and observe the performance of the two approaches at various LS value. Fig. 5(a) shows the comparison of IWFPM and IMSApriori algorithm in synthetic dataset. It is known that IWFPM is better than IMSApriori on time performance. Fig. 5(b) shows the time consumption varied with different LS value for IWFPM and IMSApriori approaches in real world dataset.

In addition, another innovation of IWFPM algorithm is to define the $R_{\text{Interest}}$, which reflects the users’ likeability to the rules. Therefore, we also compare IWFPM algorithm to DWARMMS algorithm presented in reference [22] at various minwconf by setting $LS=0.01$, $\beta=0.2$ and $\text{minInterest}=0.4$. Fig. 6(a) shows the performance of IWFPM and DWARMMS approaches for synthetic dataset, and it illustrates that the number of rules diminishes as minwconf increases. What’s more, the proposed approach excludes a large number of redundant rules and mines the interested rules with the same minwconf. Fig. 6(b) shows the performance of IWFPM and DWARMMS approaches in real world dataset.
5. Conclusion and Future Work

In this paper, we have developed the efficient mining approach to extract frequent item sets for discovering interest association rules. Our approach assigns appropriate minimum support (minsup) value and weight for all items and extends the support-confidence framework. Meanwhile, an interest measure is defined to the mining algorithm for the sake of extracting more users’ interest frequent patterns. Finally, the performances demonstrate that the proposed algorithm is superior to the existing algorithms. In the future, we are going to improve the efficiency of the algorithm and apply it in various fields. We also believe that further researches require more precise techniques to mine frequent patterns that reflecting users’ real preferences.

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